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Sr. No. of Question Paper : 7563

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Your Roll No.....

Unique Paper Code : 2271303

Name of the Paper : Statistical Methods in Economics - II

Name of the Course : B.A. (Hons.) Economics

Semester : III

Duration : 3 Hours

Maximum Marks : 75

Instructions for Candidates

1. Write your Roll No. on the top immediately on receipt of this question paper.
2. All questions within each section are to be answered in a continuous manner on the answer sheet. Start each question on a new page and all subparts of a question should follow one after the other.
3. Use of simple calculator is permitted.
4. Required statistical tables are attached with this question paper.
5. This paper contains four sections. Attempt all sections.
6. Answers may be written either in English or Hindi; but the same medium should be used throughout the paper.

छात्रों के लिए निर्देश

1. इस प्रश्न-पत्र के मिलते ही ऊपर दिए गए निर्धारित स्थान पर अपना अनुक्रमांक लिखिए।
2. प्रत्येक भाग के सभी प्रश्न के उत्तर एक साथ उत्तर पुस्तिका पर दें। प्रत्येक प्रश्न नये पेज पर और उपभागों का एक के बाद क्रम से प्रश्नों के उत्तर दीजिए।
3. साधारण कैलकुलेटर का उपयोग मान्य है।
4. इस प्रश्न पत्र के साथ स्टैटिकल टेबल संलग्न की गई है।
5. इस प्रश्न पत्र में चार खंड हैं। सभी खंडों के उत्तर दीजिए।
6. इस प्रश्न-पत्र का उत्तर अंग्रेजी या हिंदी किसी एक भाषा में दीजिए, लेकिन सभी उत्तरों का माध्यम एक ही होना चाहिए।

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Section I

Q1 is compulsory. Attempt any one From Q2 and Q3.

भाग I

प्रश्न संख्या 1 अनिवार्य है।

किन्हीं एक प्रश्न संख्या 2 और 3 को हल कीजिए।

- (a) A confectionary shop sells three types of candies priced at Rs 3.00, Rs 3.20, and Rs 3.40 per piece, respectively. Let X_1 , X_2 , and X_3 denote the number of these candies sold on a particular day. Suppose the X_i 's are independent with μ_1 , μ_2 , and μ_3 equal to 1000, 500 and 300, respectively and σ_1 , σ_2 , and σ_3 equal to 100, 80 and 50, respectively.

(i) What is the expected daily revenue of the shop from the sale of these candies?

(ii) Calculate the standard deviation of the revenue from the sale of these candies.

(iii) Would your answers be correct if the X_i 's were not independent? Explain. (4)

- (b) For the following sample data on variables x and y :

X	112.3	97.0	92.7	86.0	102.0	99.2	95.8	103.5	89.0	86.7
Y	75.0	71.0	57.7	48.7	74.3	73.3	68.0	59.3	57.8	48.5

(i) Obtain the equation of the least squares line and interpret its slope.

(ii) Calculate and interpret the coefficient of determination. (6)

- (क) एक मिठाई की दुकान तीन प्रकार की मिठाइयाँ बेचती है जिनका मूल्य क्रमशः 3.00 रु., 3.20 रु., एवं 3.40 रु. प्रति नग है। माना कि X_1 , X_2 , और X_3 किसी विशिष्ट, दिन बेची गयी मिठाइयों की संख्या को व्यक्त करते हैं। माना कि X_i के मान μ_1 , μ_2 , और μ_3 से स्वतंत्र हैं एवं क्रमशः 1000, 500 एवं 300 के बराबर हैं एवं σ_1 , σ_2 , और σ_3 क्रमशः 100, 80 एवं 50 के बराबर हैं।

- (i) इन मिठाइयों की बिक्री से दुकान की अनुमानित दैनिक आय क्या है?
- (ii) इन मिठाइयों की बिक्री से होने वाली आय के मानक विचलन का परिकलन कीजिए।
- (iii) यदि X_i के मान स्वतंत्र नहीं होते तो क्या आपके उत्तर सही होते? व्याख्या कीजिए।
- (ग) x एवं y के चरों हेतु निम्नलिखित प्रतिदर्श आंकड़ों के लिए:

X	112.3	97.0	92.7	86.0	102.0	99.2	95.8	103.5	89.0	86.7
Y	75.0	71.0	57.7	48.7	74.3	73.3	68.0	59.3	57.8	48.5

- (i) least squares line का समीकरण ज्ञात कीजिए एवं उसकी प्रवणता की व्याख्या कीजिए।
- (ii) निर्धारण गुणांक का परिकलन कीजिए एवं उसकी व्याख्या कीजिए।
2. (a) The time take by a randomly selected student to fill a form has a normal distribution with mean value 10 min and standard deviation 2 min. If five students fill a form on one day and six on another day, what is the probability that the sample average amount of time taken on each day is at most 11 min? (5)

(b) For the following summary statistics:

$$n=15, \sum x_i = 1640.1, \sum y_i = 299.8, \sum x_i^2 = 179,849.73$$

$$\sum y_i^2 = 6430.06, \sum x_i y_i = 32,308.59$$

- (i) Obtain the equation of the estimated regression line of y on x .
- (ii) Use the estimated line used to predict y when x is 135.
- (iii) Calculate and interpret a point estimate of σ .
- (iv) What are the values of SSE and SST?
- (v) What proportion of observed variation in y can be attributed to the approximate linear relationship between x and y ? (10)

(क) यादृच्छिक रूप से चयनित किए गए छात्रों द्वारा एक प्रपत्र को भरने में लिया गया समय 10 मिनट के माध्य मान एवं 2 मिनट के मानक विचलन के साथ प्रसामान्य बंटन को प्रदर्शित करता है। यदि एक दिन पांच छात्र प्रपत्र भरते हैं एवं दूसरे दिन छः छात्र प्रपत्र भरते हैं तो, प्रपत्र भरने में प्रतिदिन लिए गए समय की प्रतिदर्श औसत मात्र अधिकतम 11 मिनट होने की प्रायिकता क्या है?

(ख) निम्नलिखित सारांशिकृत आँकड़ों के लिए:

$$n = 15, \sum x_i = 1640.1, \sum y_i = 299.8, \sum x_i^2 = 179,849.73$$

$$\sum y_i^2 = 6430.06, \sum x_i y_i = 32,308.59$$

(i) x पर y की अनुमानित समाश्रयण रेखा का समीकरण प्राप्त कीजिए।

(ii) y का अनुमान लगाने के लिए अनुमानित रेखा का उपयोग कीजिए जब कि x का मान 135 है।

(iii) σ के बिंदु आकल का परिकलन कीजिए एवं व्याख्या कीजिए।

(iv) SSE एवं SST के मान क्या हैं?

(v) y में प्रेक्षित विचरण के किस अनुपात को x एवं y के बीच अनुमानित रैखिक संबंध के लिए जिम्मेदार ठहराया जा सकता है?

3. (a) A College has three administrative departments each having two employees. Information regarding their monthly salaries (thousands of Rs) is as follows:

Department	1	1	2	2	3	3
Employee	1	2	3	4	5	6
Salary	30	34	28	32	42	22

Suppose one of the three departments is randomly selected. Let X_1 and X_2 denote the salaries of the two employees. Determine the sampling distribution of \bar{X} . Where is this distribution centered? (5)

(b) Following summary statistics are given to explain the relationship between y and x :

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$$\sum x_i = 659, \sum x_i^2 = 28,967.50, \bar{x} = 36.6111, S_{xx} = 4840.7778,$$

$$\sum y_i = 293.2, \sum x_i y_i = 9293.95, \sum y_i^2 = 5335.76,$$

$$\hat{\beta}_1 = -0.2976, \hat{\beta}_0 = 27.183, SSE = 131.2402,$$

$$r^2 = 0.766, s = 2.8640$$

Calculate a prediction interval for y with a prediction level of 95% when x is 45. (5)

(c) Show that the "point of averages" (\bar{x}, \bar{y}) lies on the estimated regression line. (5)

(क) एक कॉलेज में तीन प्रशासनिक विभाग हैं जिनमें से प्रत्येक में दो कर्मचारी हैं। उनके मासिक वेतनों (हजार रुपयों में) के संबंध में जानकारी इस प्रकार है:

विभाग	1	1	2	2	3	3
कर्मचारी	1	2	3	4	5	6
वेतन	30	34	28	32	42	22

माना कि तीन में से एक विभाग का यादृच्छिक रूप से चयन किया जाता है। माना कि X_1 और X_2 दो कर्मचारियों के वेतन को व्यक्त करते हैं। \bar{X} के प्रतिचयन बंटन को निर्धारित कीजिए। यह बंटन कहाँ केन्द्रित है?

(ख) y एवं x के बीच संबंध की व्याख्या करने के लिए निम्नलिखित सारांश आंकड़े दिए गए हैं:

$$\sum x_i = 659, \sum x_i^2 = 28,967.50, \bar{x} = 36.6111, S_{xx} = 4840.7778,$$

$$\sum y_i = 293.2, \sum x_i y_i = 9293.95, \sum y_i^2 = 5335.76,$$

$$\hat{\beta}_1 = -0.2976, \hat{\beta}_0 = 27.183, SSE = 131.2402,$$

$$r^2 = 0.766, s = 2.8640$$

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95% के प्रागुक्ति स्तर के साथ ल के लिए प्रागुक्ति अंतराल का परिकलन कीजिए जबकि x का मान 45 है।

- (ग) प्रदर्शित कीजिए कि “औसत बिंदु (point of averages) (\bar{x}, \bar{y}) अनुमानित समाश्रयण रेखा (regression line) पर अवस्थित हैं।

SECTION II

ATTEMPT ALL QUESTIONS

भाग II

सभी प्रश्नों को हल कीजिए

4. (a) Explain properties of a good estimator. Consider a random sample $(X_1, X_2, X_3, \dots, X_n)$ from a population from a probability distribution function $f(x; \theta)$. If Expected value of an estimator $\hat{\theta}$ is equal to $(n/n+1) * \theta$, what is the bias of this estimator? Find an estimator that is unbiased. (3+2)

- (b) Consider a random sample $(X_1, X_2, X_3, \dots, X_n)$ from a population from a probability distribution function

$$f(x; \theta) = 0.5(1 + x * \theta). \text{ Where } -1 \leq x \leq 1.$$

- (i) Show that $\hat{\theta} = 3 * \text{sample mean}$ is an unbiased estimator for σ .

- (ii) If a sample size is 3 and the sample is $(-1, 0, 2)$ give point estimate for θ . (4+1)

- (c) Let (x_1, x_2, \dots, x_n) be a random sample from a population with mean μ and standard deviation σ . Show that $S^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1}$ is unbiased estimator of population variance, denoted by σ^2 .

(5)

- (d) From a survey of 500 families, 340 were reported to like Star Plus channel.

Find a 90% confidence interval for the proportion of families that like Star Plus channel. What is the required sample size if we want to be 95% confident that our estimate of the proportion of families that like Star plus channel is within 0.02 of the true proportion? (5)

- (e) Let X be a continuous random variable that is uniformly distributed over $(0, A)$. Find the moment estimator of A . (3+2)

{क} अच्छे प्राक्कलक के गुणों की व्याख्या कीजिए। प्रायिकता वितरण फलन $(x; \theta)$ से एक समष्टि के यादृच्छिक प्रतिदर्श $(X_1, X_2, X_3, \dots, X_n)$ पर विचार कीजिए। यदि प्राक्कलक $\hat{\theta}$ का अपेक्षित मान $(n/n+1) * \theta$ के समतुल्य है, तो इस प्राक्कलक की अभिनति क्या है? ऐसा प्राक्कलक ज्ञात कीजिए जो अनभिन्न है।

{ख} एक समष्टि के यादृच्छिक प्रतिदर्श $(X_1, X_2, X_3, \dots, X_n)$ पर विचार कीजिए जिसका प्रायिकता वितरण फलन इस प्रकार है:

$$f(x; \theta) = 0.5(1 + x * \theta). \text{ जहाँ } -1 \leq x \leq 1.$$

(i) प्रदर्शित कीजिए कि $\hat{\theta} = 3 * \text{प्रतिदर्श माध्य } \theta$ के लिए अनभिन्न प्राक्कलक है।

(ii) यदि प्रतिदर्श आकार 3 है एवं प्रतिदर्श $(-1, 0, 2)$ है, तो θ के लिए बिंदु आकलन प्रदान कीजिए।

{ग} माना कि माध्य - एवं मानक विचलन σ की समष्टि से लिया गया एक यादृच्छिक प्रतिदर्श (x_1, x_2, \dots, x_n) है। प्रदर्शित कीजिए कि $S^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1}$ ऐसे समष्टि प्रसरण (population variance) का अनभिन्न प्राक्कलक है जिसे σ^2 से व्यक्त किया जाता है।

{घ} 500 परिवारों के सर्वेक्षण से यह रिपोर्ट प्राप्त हुई कि 340 परिवार स्टार प्लस को पसंद करते थे। स्टार प्लस चैनल को पसंद करने वाले परिवारों के लिए 90% विश्वास्यता अंतराल को ज्ञात कीजिए। यदि हम 95% सुनिश्चित होना चाहते हैं कि स्टार प्लस चैनल को पसंद करने वाले परिवारों का हमारा अनुमान वास्तविक अनुपात के 0.02 के अंतर्गत है तो वांछित प्रतिदर्श आकार क्या है?

{ङ} माना कि X संतत याणक्षिक चर है जो $(0, A)$ पर समान रूप से वितरित है। A का आधूँर प्राक्कलक (moment estimator) ज्ञात कीजिए।

SECTION III

Q5 IS COMPULSORY. ATTEMPT ANY TWO QUESTIONS OUT OF Q6, Q7 AND Q8.

भाग III

प्रश्न 5 अनिवार्य है। प्र.6, प्र.7 एवं प्र.8 में से

कोई दो प्रश्न हल कीजिए।

5. What are the two types of errors in hypothesis testing? For a given sample size, can both errors be simultaneously reduced? Explain with the help of diagram. (5)

परिकल्पना परीक्षण (hypothesis testing) में दो प्रकार की त्रुटियाँ कौन सी हैं? क्या दिए गए प्रतिदर्श आकार के लिए दोनों त्रुटियों को एक साथ कम किया जा सकता है? आरेख की सहायता से समझाइए।

6. (a) A professor believes that a standard deviation of about 13 points on a hundred point exam indicates that the exam does a good job. He gave an exam to his class of 31 students. The mean score was 72.7 and standard deviation was 15.9. Does this exam meet the goodness criterion? Use $\alpha = 0.10$.

- (b) For each of the following pairs of hypothesis indicate if the rules of setting up hypothesis are followed. If not, give reasons.

- | | | |
|-------------------------|---------------------|-------|
| (i) $H_0: \mu = 100$ | $H_1: \mu \leq 100$ | |
| (ii) $H_0: \mu \neq 21$ | $H_1: \mu < 21$ | |
| (iii) $H_0: \mu = 12.5$ | $H_1: \mu < 12.8$ | |
| (iv) $H_0: \mu > 100$ | $H_1: \mu \neq 100$ | |
| (v) $H_0: \mu > 100$ | $H_1: \mu = 100$ | (5+5) |

- (क) एक प्रोफेसर का विश्वास है कि 100 अंकों की परीक्षा में लगभग 13 अंकों का मानक विचलन यह इंगित करता है कि परीक्षा अच्छा कार्य करती है। उसने 31 छात्रों की अपनी कक्षा की एक परीक्षा ली। माध्य प्राप्तांक 72.7 थे एवं मानक विचलन 15.9 था। क्या यह परीक्षा अच्छाई के मानदण्ड (goodness criterion) को पूरा करती है। $\alpha = 0.10$ का प्रयोग कीजिए।

(ख) निम्नलिखित में से परिकल्पना के प्रत्येक युग्म के लिए इंगित कीजिए कि क्या परिकल्पना की स्थापना के नियमों का पालन किया जाता है। यदि नहीं तो कारण बताइए।

$$(i) H_0: \mu = 100 \quad H_1: \mu \leq 100$$

$$(ii) H_0: \mu \neq 21 \quad H_1: \mu < 21$$

$$(iii) H_0: \mu = 12.5 \quad H_1: \mu < 12.8$$

$$(iv) H_0: \mu > 100 \quad H_1: \mu \neq 100$$

$$(v) H_0: \mu > 100 \quad H_1: \mu = 100$$

7. (a) A quality inspector picks up 100 masks from the market to note that 14 do not work as they are unable to filter out air impurities. The manufacturer claims that only 10% of masks are unable to filter out air impurities. Using a significance level of 98% can the manufacturer's claim be supported? What is the p value of your test?
- (b) A consultant needs to compare two populations, but he needs to know if the variances are same for them before he proceeds. He collects samples of size 10 from both populations to get standard deviations of 12.2 and 15.4. Using a 95% confidence level test for equality of variances in both populations.
- (5+5)

(क) एक गुणवत्ता निरीक्षक बाजार से 100 मास्क उठाता है और उसे ज्ञात होता है कि उनमें से 14 मास्क कार्य नहीं कर रहे हैं क्योंकि वे वायु की अशुद्धियों का निस्पंदन करने में असमर्थ हैं। विनिर्माता का दावा है कि केवल 10% मास्क ही वायु की अशुद्धियों का निस्पंदन करने में असमर्थ हैं। 98% के सार्थकता स्तर का उपयोग कर क्या विनिर्माता के दावे का समर्थन किया जा सकता है? आपके परीक्षण का p मान क्या है?

(ख) एक सलाहकार को दो समष्टियों की तुलना करने की आवश्यकता है, किन्तु यह कार्य आरम्भ करने से पहले वह ज्ञात करना चाहता है कि क्या उनके लिए प्रसरण समान हैं। वह 12.2 और 15.4 का मानक विचलन प्राप्त करने के लिए दोनों समष्टियों से 10 के आकार के प्रतिदर्श एकत्रित करता है। 95% विश्वास स्तर का प्रयोग कर दोनों समष्टियों में प्रसरणों की समानता का परीक्षण कीजिए।

8. (a) A consultancy firm wants to check if average wages across males and females are different. They took samples that reveal the following information:

Males	Females
Mean = 62.5	Mean = 39.7
Standard deviation = 23.7	Standard deviation = 8.9
Size = 175	Size = 168

- (i) Using a 90% confidence level can we argue that there is no difference in wages across males and females? Assume equal population variances.
- (ii) Can we argue that males earn more than females, using a 98% confidence level?
- (b) The CEO and HR head of a company argue over the no of yearly holidays taken by employees. The HR head argues that on average employees take more than 40 holidays in a year. To test this claim a sample of 15 employees is taken and sample average is found to be 41.17 with standard deviation is 4.71. Test the HR head's claim that employees take more than 40 yearly holidays at a 0.05 level of significance. (5+5)

(क) एक कंसल्टेंसी फर्म यह जाँच करना चाहती है कि क्या पुरुषों और महिलाओं के बीच औसत पारिश्रमिक भिन्न है। वे प्रतिदर्श ग्रहण करते हैं जो निम्नलिखित जानकारी प्रकट करते हैं:

पुरुष	महिला
माध्य = 62.5	माध्य = 39.7
मानक विचलन = 23.7	मानक विचलन = 8.9
आकार = 175	आकार = 168

- (i) 90% विश्वास स्तर का प्रयोग कर क्या हम यह तर्क कर सकते हैं कि पुरुषों एवं महिलाओं के पारिश्रमिक में कोई अंतर नहीं है। समष्टि प्रसरणों को समतुल्य मान लीजिए।
- (ii) 98% विश्वास स्तर का प्रयोग कर क्या हम यह तर्क कर सकते हैं कि पुरुष महिलाओं की तुलना में अधिक अर्जित करते हैं?
- (ख) कम्पनी के मुख्य कार्यकारी अधिकारी (CEO) एवं कम्पनी के एच.आर. प्रमुख कर्मचारियों द्वारा लिए गए वार्षिक अवकाशों के संबंध में तर्क करते हैं। एच.आर. प्रमुख का तर्क है कि औसत रूप से कर्मचारी वर्ष में 40 से अधिक अवकाश लेते हैं। इस दावे का परीक्षण करने के लिए 15 कर्मचारियों का एक प्रतिदर्श लिया जाता है एवं प्रतिदर्श का औसत 4.71 के मानक विचलन के साथ 41.17 पाया जाता है। एच.आर. प्रमुख के दावे का परीक्षण कीजिए कि कर्मचारी 0.05 के सार्थकता स्तर पर 40 से अधिक अवकाश लेते हैं।

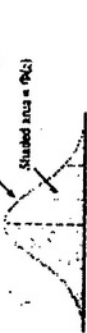
z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
0.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753
0.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141
0.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517
0.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879
0.5	.6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224
0.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549
0.7	.7580	.7611	.7642	.7673	.7704	.7734	.7764	.7794	.7823	.7852
0.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133
0.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8829
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9278	.9292	.9306	.9319
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9685	.9693	.9699	.9706
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9858
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952
2.6	.9953	.9955	.9956	.9957	.9958	.9959	.9961	.9962	.9963	.9964
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974
2.8	.9975	.9976	.9977	.9978	.9979	.9980	.9981	.9982	.9983	.9984
2.9	.9985	.9986	.9987	.9988	.9989	.9990	.9991	.9992	.9993	.9994
3.0	.9995	.9996	.9997	.9998	.9999	.9999	.9999	.9999	.9999	.9999
3.1	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999
3.2	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999
3.3	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999
3.4	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999	.9999

Table A.3 Standard Normal Curve Areas (cont.)

Table A.3 Standard Normal Curve Areas

$$\phi(z) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{z^2}{2\sigma^2}}$$

Standard normal density function



z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
-3.4	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0002
-3.3	.0005	.0005	.0005	.0004	.0004	.0004	.0004	.0004	.0004	.0003
-3.2	.0007	.0007	.0006	.0006	.0006	.0006	.0006	.0006	.0005	.0005
-3.1	.0010	.0009	.0009	.0008	.0008	.0008	.0008	.0007	.0007	.0007
-3.0	.0013	.0013	.0013	.0012	.0012	.0011	.0011	.0010	.0010	.0010
-2.9	.0016	.0016	.0016	.0015	.0015	.0014	.0014	.0013	.0013	.0013
-2.8	.0019	.0019	.0018	.0018	.0017	.0017	.0016	.0016	.0015	.0015
-2.7	.0023	.0023	.0022	.0022	.0021	.0021	.0020	.0020	.0019	.0019
-2.6	.0027	.0027	.0026	.0026	.0025	.0024	.0024	.0023	.0023	.0022
-2.5	.0031	.0031	.0030	.0030	.0029	.0028	.0028	.0027	.0026	.0026
-2.4	.0036	.0036	.0035	.0034	.0034	.0033	.0032	.0032	.0031	.0031
-2.3	.0041	.0041	.0040	.0039	.0038	.0038	.0037	.0036	.0036	.0035
-2.2	.0046	.0046	.0045	.0044	.0043	.0042	.0041	.0041	.0040	.0040
-2.1	.0051	.0051	.0050	.0049	.0048	.0047	.0046	.0045	.0045	.0044
-2.0	.0054	.0054	.0053	.0052	.0051	.0050	.0049	.0048	.0047	.0047
-1.9	.0058	.0058	.0057	.0056	.0055	.0054	.0053	.0052	.0051	.0051
-1.8	.0062	.0062	.0061	.0060	.0059	.0058	.0057	.0056	.0055	.0055
-1.7	.0066	.0066	.0065	.0064	.0063	.0062	.0061	.0060	.0059	.0059
-1.6	.0070	.0070	.0069	.0068	.0067	.0066	.0065	.0064	.0063	.0063
-1.5	.0074	.0074	.0073	.0072	.0071	.0070	.0069	.0068	.0067	.0067
-1.4	.0078	.0078	.0077	.0076	.0075	.0074	.0073	.0072	.0071	.0071
-1.3	.0082	.0082	.0081	.0080	.0079	.0078	.0077	.0076	.0075	.0075
-1.2	.0086	.0086	.0085	.0084	.0083	.0082	.0081	.0080	.0079	.0079
-1.1	.0090	.0090	.0089	.0088	.0087	.0086	.0085	.0084	.0083	.0083
-1.0	.0094	.0094	.0093	.0092	.0091	.0090	.0089	.0088	.0087	.0087
-0.9	.0098	.0098	.0097	.0096	.0095	.0094	.0093	.0092	.0091	.0091
-0.8	.0102	.0102	.0101	.0100	.0099	.0098	.0097	.0096	.0095	.0095
-0.7	.0106	.0106	.0105	.0104	.0103	.0102	.0101	.0100	.0099	.0099
-0.6	.0110	.0110	.0109	.0108	.0107	.0106	.0105	.0104	.0103	.0103
-0.5	.0114	.0114	.0113	.0112	.0111	.0110	.0109	.0108	.0107	.0107
-0.4	.0118	.0118	.0117	.0116	.0115	.0114	.0113	.0112	.0111	.0111
-0.3	.0122	.0122	.0121	.0120	.0119	.0118	.0117	.0116	.0115	.0115
-0.2	.0126	.0126	.0125	.0124	.0123	.0122	.0121	.0120	.0119	.0119
-0.1	.0130	.0130	.0129	.0128	.0127	.0126	.0125	.0124	.0123	.0123
0.0	.0134	.0134	.0133	.0132	.0131	.0130	.0129	.0128	.0127	.0127

(Continued)

Appendix Tables 573

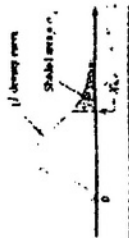


Table A.7 Critical Values for Chi-Squared Distributions

df	.99	.95	.90	.85	.80	.75	.70	.65	.60	.55	.50	.45	.40	.35	.30	.25	.20	.15	.10	.05	.025	.01	.005
1	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
2	0.010	0.020	0.051	0.072	0.102	0.138	0.175	0.215	0.259	0.300	0.343	0.389	0.438	0.489	0.542	0.597	0.654	0.713	0.774	0.837	0.901	0.966	1.032
3	0.016	0.032	0.081	0.115	0.155	0.197	0.241	0.288	0.337	0.389	0.443	0.499	0.557	0.617	0.679	0.743	0.809	0.877	0.947	1.019	1.093	1.169	1.246
4	0.020	0.040	0.093	0.130	0.174	0.220	0.268	0.318	0.370	0.424	0.480	0.538	0.598	0.660	0.724	0.790	0.858	0.928	0.999	1.072	1.147	1.223	1.300
5	0.024	0.048	0.104	0.143	0.190	0.238	0.288	0.340	0.393	0.448	0.504	0.561	0.620	0.680	0.742	0.805	0.870	0.937	1.005	1.079	1.154	1.230	1.307
6	0.027	0.054	0.111	0.151	0.200	0.250	0.301	0.354	0.407	0.462	0.518	0.575	0.634	0.694	0.756	0.819	0.884	0.951	1.019	1.094	1.170	1.246	1.323
7	0.029	0.058	0.117	0.158	0.208	0.259	0.311	0.364	0.417	0.472	0.528	0.585	0.644	0.704	0.766	0.829	0.894	0.961	1.029	1.104	1.180	1.256	1.333
8	0.031	0.060	0.120	0.161	0.212	0.263	0.315	0.368	0.421	0.476	0.532	0.589	0.648	0.708	0.770	0.833	0.898	0.965	1.033	1.108	1.184	1.260	1.337
9	0.032	0.062	0.122	0.163	0.214	0.265	0.317	0.370	0.423	0.478	0.534	0.591	0.650	0.710	0.772	0.835	0.899	0.966	1.034	1.109	1.185	1.261	1.338
10	0.033	0.063	0.123	0.164	0.215	0.266	0.318	0.371	0.424	0.479	0.535	0.592	0.651	0.711	0.773	0.836	0.900	0.967	1.035	1.110	1.186	1.262	1.339
11	0.034	0.064	0.124	0.165	0.216	0.267	0.319	0.372	0.425	0.480	0.536	0.593	0.652	0.712	0.774	0.837	0.901	0.968	1.036	1.111	1.187	1.263	1.340
12	0.035	0.065	0.125	0.166	0.217	0.268	0.320	0.373	0.426	0.481	0.537	0.594	0.653	0.713	0.775	0.838	0.902	0.969	1.037	1.112	1.188	1.264	1.341
13	0.036	0.066	0.126	0.167	0.218	0.269	0.321	0.374	0.427	0.482	0.538	0.595	0.654	0.714	0.776	0.839	0.903	0.970	1.038	1.113	1.189	1.265	1.342
14	0.037	0.067	0.127	0.168	0.219	0.270	0.322	0.375	0.428	0.483	0.539	0.596	0.655	0.715	0.777	0.840	0.904	0.971	1.039	1.114	1.190	1.266	1.343
15	0.037	0.067	0.127	0.168	0.219	0.270	0.322	0.375	0.428	0.483	0.539	0.596	0.655	0.715	0.777	0.840	0.904	0.971	1.039	1.114	1.190	1.266	1.343
16	0.038	0.068	0.128	0.169	0.220	0.271	0.323	0.376	0.429	0.484	0.540	0.597	0.656	0.716	0.778	0.841	0.905	0.972	1.040	1.115	1.191	1.267	1.344
17	0.038	0.068	0.128	0.169	0.220	0.271	0.323	0.376	0.429	0.484	0.540	0.597	0.656	0.716	0.778	0.841	0.905	0.972	1.040	1.115	1.191	1.267	1.344
18	0.039	0.069	0.129	0.170	0.221	0.272	0.324	0.377	0.430	0.485	0.541	0.598	0.657	0.717	0.779	0.842	0.906	0.973	1.041	1.116	1.192	1.268	1.345
19	0.039	0.069	0.129	0.170	0.221	0.272	0.324	0.377	0.430	0.485	0.541	0.598	0.657	0.717	0.779	0.842	0.906	0.973	1.041	1.116	1.192	1.268	1.345
20	0.040	0.070	0.130	0.171	0.222	0.273	0.325	0.378	0.431	0.486	0.542	0.599	0.658	0.718	0.780	0.843	0.907	0.974	1.042	1.117	1.193	1.269	1.346
21	0.040	0.070	0.130	0.171	0.222	0.273	0.325	0.378	0.431	0.486	0.542	0.599	0.658	0.718	0.780	0.843	0.907	0.974	1.042	1.117	1.193	1.269	1.346
22	0.040	0.070	0.130	0.171	0.222	0.273	0.325	0.378	0.431	0.486	0.542	0.599	0.658	0.718	0.780	0.843	0.907	0.974	1.042	1.117	1.193	1.269	1.346
23	0.041	0.071	0.131	0.172	0.223	0.274	0.326	0.379	0.432	0.487	0.543	0.600	0.659	0.719	0.781	0.844	0.908	0.975	1.043	1.118	1.194	1.270	1.347
24	0.041	0.071	0.131	0.172	0.223	0.274	0.326	0.379	0.432	0.487	0.543	0.600	0.659	0.719	0.781	0.844	0.908	0.975	1.043	1.118	1.194	1.270	1.347
25	0.041	0.071	0.131	0.172	0.223	0.274	0.326	0.379	0.432	0.487	0.543	0.600	0.659	0.719	0.781	0.844	0.908	0.975	1.043	1.118	1.194	1.270	1.347
26	0.041	0.071	0.131	0.172	0.223	0.274	0.326	0.379	0.432	0.487	0.543	0.600	0.659	0.719	0.781	0.844	0.908	0.975	1.043	1.118	1.194	1.270	1.347
27	0.042	0.072	0.132	0.173	0.224	0.275	0.327	0.380	0.433	0.488	0.544	0.601	0.660	0.720	0.782	0.845	0.909	0.976	1.044	1.119	1.195	1.271	1.348
28	0.042	0.072	0.132	0.173	0.224	0.275	0.327	0.380	0.433	0.488	0.544	0.601	0.660	0.720	0.782	0.845	0.909	0.976	1.044	1.119	1.195	1.271	1.348
29	0.042	0.072	0.132	0.173	0.224	0.275	0.327	0.380	0.433	0.488	0.544	0.601	0.660	0.720	0.782	0.845	0.909	0.976	1.044	1.119	1.195	1.271	1.348
30	0.042	0.072	0.132	0.173	0.224	0.275	0.327	0.380	0.433	0.488	0.544	0.601	0.660	0.720	0.782	0.845	0.909	0.976	1.044	1.119	1.195	1.271	1.348
31	0.042	0.072	0.132	0.173	0.224	0.275	0.327	0.380	0.433	0.488	0.544	0.601	0.660	0.720	0.782	0.845	0.909	0.976	1.044	1.119	1.195	1.271	1.348
32	0.042	0.072	0.132	0.173	0.224	0.275	0.327	0.380	0.433	0.488	0.544	0.601	0.660	0.720	0.782	0.845	0.909	0.976	1.044	1.119	1.195	1.271	1.348
33	0.042	0.072	0.132	0.173	0.224	0.275	0.327	0.380	0.433	0.488	0.544	0.601	0.660	0.720	0.782	0.845	0.909	0.976	1.044	1.119	1.195	1.271	1.348
34	0.042	0.072	0.132	0.173	0.224	0.275	0.327	0.380	0.433	0.488	0.544	0.601	0.660	0.720	0.782	0.845	0.909	0.976	1.044	1.119	1.195	1.271	1.348
35	0.042	0.072	0.132	0.173	0.224	0.275	0.327	0.380	0.433	0.488	0.544	0.601	0.660	0.720	0.782	0.845	0.909	0.976	1.044	1.119	1.195	1.271	1.348
36	0.042	0.072	0.132	0.173	0.224	0.275	0.327	0.380	0.433	0.488	0.544	0.601	0.660	0.720	0.782	0.845	0.909	0.976	1.044	1.119	1.195	1.271	1.348
37	0.042	0.072	0.132	0.173	0.224	0.275	0.327	0.380	0.433	0.488	0.544	0.601	0.660	0.720	0.782	0.845	0.909	0.976	1.044	1.119	1.195	1.271	1.348
38	0.042	0.072	0.132	0.173	0.224	0.275	0.327	0.380	0.433	0.488	0.544	0.601	0.660	0.720	0.782	0.845	0.909	0.976	1.044	1.119	1.195	1.271	1.348
39	0.042	0.072	0.132	0.173	0.224	0.275	0.327	0.380	0.433	0.488	0.544	0.601	0.660	0.720	0.782	0.845	0.909	0.976	1.044	1.119	1.195	1.271	1.348
40	0.042	0.072	0.132	0.173	0.224	0.275	0.327	0.380	0.433	0.488	0.544	0.601	0.660	0.720	0.782	0.845	0.909	0.976	1.044	1.119	1.195	1.271	1.348

$$F_{\alpha/2, df_1, df_2} = \frac{1}{F_{1-\alpha/2, df_2, df_1}}$$

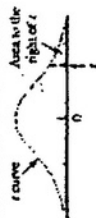
Appendix Tables 571



Table A.5 Critical Values for t Distributions

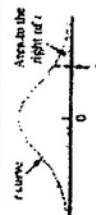
P	.99	.95	.90	.85	.80	.75	.70	.65	.60	.55	.50	.45	.40	.35	.30	.25	.20	.15	.10	.05	.025	.01	.005	.001
1	3.078	6.314	12.706	18.821	24.303	29.200	33.623	37.657	41.331	44.645	47.659	50.441	52.954	55.241	57.251	59.036	60.657	62.151	63.557	64.894	66.171	67.397	68.581	
2	1.826	2.920	4.303	5.865	7.500	9.200	10.954	12.746	14.561	16.388	18.226	20.073	21.928	23.790	25.658	27.531	29.408	31.289	33.173	35.060	36.950	38.842	40.736	
3	1.603	2.553	3.822	5.241	6.700	8.200	9.734	11.291	12.860	14.440	16.030	17.630	19.240	20.859	22.487	24.124	25.770	27.425	29.089	30.761	32.441	34.128	35.822	
4	1.453	2.332	3.516	4.847	6.210	7.600	9.014	10.441	11.880	13.330	14.790	16.260	17.740	19.230	20.730	22.240	23.760	25.290	26.830	28.380	29.940	31.510	33.080	
5	1.476	2.015	3.171	4.447	5.740	7.060	8.400	9.750	11.110	12.480	13.860	15.250	16.650	18.060	19.480	20.910	22.350	23.800	25.260	26.730	28.210	29.700	31.200	
6	1.440	1.943	3.083	4.347	5.620	6.910	8.210	9.520	10.840	12.170	13.510	14.860	16.220	17.590	18.970	20.360	21.760	23.170	24.590	26.020	27.460	28.910	30.370	
7	1.415	1.895	3.025	4.283	5.540	6.810	8.090	9.380	10.680	11.990	13.300	14.620	15.950	17.290	18.640	19.990	21.350	22.720	24.100	25.490	26.890	28.300	29.720	
8	1.397	1.860	2.985	4.237	5.480	6.730	7.980	9.240	10.510	11.780	13.060	14.350	15.650	16.960	18.280	19.610	20.950	22.300	23.660	25.030	26.410	27.800	29.200	
9	1.383	1.833	2.953	4.203	5.440	6.680	7.920	9.170	10.430	11.690	12.960	14.240	15.530	16.830	18.140	19.460	20.790	22.130	23.480	24.840	26.210	27.590	28.980	
10	1.372	1.812	2.932	4.182	5.410	6.650	7.890	9.140	10.390	11.640	12.900	14.170	15.450	16.740	18.040	19.350	20.670	22.000	23.340	24.690	26.050	27.420	28.800	
11	1.363	1.798	2.921	4.172	5.390	6.630	7.870	9.110	10.350	11.590	12.840	14.090	15.350	16.620	17.890	19.170	20.460	21.760	23.070	24.390	25.720	27.060	28.410	
12	1.358	1.786	2.910	4.162	5.380	6.610	7.850	9.090	10.320	11.550	12.790	14.030	15.280	16.540	17.800	19.070	20.350	21.640	22.940	24.250	25.570	26.900	28.240	
13	1.350	1.771	2.900	4.152	5.370	6.590	7.830	9.060	10.280	11.500	12.730	13.960	15.190	16.430	17.670	18.920	20.180	21.450	22.730	24.020	25.320	26.630	27.950	
14	1.343	1.761	2.890	4.142	5.360	6.580	7.810	9.030	10.250	11.460	12.680	13.900	15.120	16.350	17.580	18.820	20.070	21.330	22.600	23.880	25.170	26.470	27.780	
15	1.341	1.753	2.883	4.134	5.353	6.573	7.803	8.993	10.220	11.420	12.630	13.840	15.050	16.260	17.470	18.680	19.890	21.110	22.340	23.570	24.800	26.030	27.260	
16	1.337	1.744	2.876	4.126	5.346	6.566	7.796	8.976	10.190	11.380	12.580	13.780	14.980	16.180	17.380	18.580	19.780	20.990	22.200	23.410	24.620	25.830	27.040	
17	1.333	1.740	2.871	4.122	5.342	6.562	7.792	8.972	10.170	11.350	12.550	13.750	14.940	16.130	17.320	18.510	19.700	20.890	22.080	23.270	24.460	25.650	26.840	
18	1.330	1.734	2.867	4.118	5.338	6.558	7.788	8.968	10.150	11.320	12.510	13.700	14.890	16.070	17.250	18.430	19.610	20.790	21.960	23.130	24.300	25.470	26.640	
19	1.328	1.732	2.865	4.116	5.336	6.556	7.786	8.966	10.140	11.300	12.490	13.680	14.860	16.040	17.210	18.380	19.550	20.720	21.880	23.040	24.190	25.340	26.490	
20	1.325	1.729	2.863	4.114	5.334	6.554	7.784	8.964	10.130	11.280	12.460	13.640	14.810	15.980	17.140	18.300	19.450	20.600	21.750	22.890	24.030	25.160	26.290	
21	1.323	1.727	2.861	4.112	5.332	6.552	7.782	8.962	10.120	11.260	12.430	13.600	14.760	15.920	17.070	18.220	19.360	20.500	21.630	22.760	23.880	25.000	26.110	
22	1.321	1.717	2.859	4.110	5.330	6.550	7.780	8.960	10.110	11.240	12.400	13.560	14.710	15.860	17.000	18.140	19.270	20.390	21.510	22.620	23.730	24.830	25.930	
23	1.319	1.714	2.857	4.108	5.328	6.548	7.778	8.958	10.100	11.220	12.370	13.520	14.660	15.800	16.930	18.050	19.160	20.260	21.360	22.450	23.540	24.620	25.700	
24	1.318	1.711	2.856	4.107	5.327	6.547	7.777	8.957	10.090	11.210	12.360	13.500	14.640	15.770	16.890	18.000	19.090	20.180	21.260	22.340	23.410	24.480	25.550	
25	1.316	1.703	2.854	4.105	5.325	6.546	7.775	8.955	10.080	11.190	12.340	13.470	14.600	15.720	16.830	17.930	19.020	20.100	21.170	22.240	23.300	24.360	25.410	
26	1.315	1.706	2.856	4.106	5.326	6.547	7.776	8.956	10.081	11.191	12.341	13.471	14.591	15.711	16.811	17.901	18.981	20.051	21.111	22.161	23.211	24.251	25.291	
27	1.314	1.703	2.855	4.105	5.325	6.546	7.775	8.955	10.080	11.189	12.339	13.469	14.589	15.709	16.809	17.899	18.979	20.049	21.109	22.159	23.209	24.249	25.289	
28	1.313	1.701	2.854	4.104	5.324	6.545	7.774	8.954	10.079	11.188	12.338	13.468	14.588	15.708	16.808	17.898	18.978	20.048	21.108	22.158	23.208	24.248	25.288	
29	1.311	1.699	2.853	4.103	5.323	6.544	7.773	8.953	10.078	11.187	12.337	13.467	14.587	15.707	16.807	17.897	18.977	20.047	21.107	22.157	23.207	24.247	25.287	
30	1.310	1.697	2.852	4.102	5.322	6.543	7.772	8.952	10.077	11.186	12.336	13.466	14.586	15.706	16.806	17.896	18.976	20.046	21.106	22.156	23.206	24.246	25.286	
31	1.309	1.694	2.851	4.101	5.321	6.542	7.771	8.951	10.076	11.185	12.335	13.465	14.585	15.705	16.805	17.895	18.975	20.045	21.105	22.155	23.205	24.245	25.285	
32	1.307	1.691	2.850	4.100	5.320	6.541	7.770	8.950	10.075	11.184	12.334	13.464	14.584	15.704	16.804	17.894	18.974	20.044	21.104	22.154	23.204	24.244	25.284	
33	1.307	1.691	2.850	4.100	5.320	6.541	7.770	8.950	10.075	11.184	12.334	13.464	14.584	15.704	16.804	17.894	18.974	20.044	21.104	22.154	23.204	24.244	25.284	
34	1.306	1.689	2.849	4.099	5.319	6.540	7.769	8.949	10.074	11.183	12.333	13.463	14.583	15.703	16.803	17.893	18.973	20.043	21.103	22.153	23.203	24.243	25.283	
35	1.305	1.688	2.848	4.098	5.318	6.539	7.768	8.948	10.073	11.182	12.332	13.462	14.582	15.702	16.802	17.892	18.972	20.042	21.102	22.152	23.202	24.242	25.282	
36	1.304	1.687	2.847	4.097	5.317	6.538	7.767	8.947	10.072	11.181	12.331	13.461	14.581	15.701	16.801	17.891	18.971	20.041	21.101	22.151	23.201	24.241	25.281	
37	1.304	1.686	2.846	4.096	5.316	6.537	7.766	8.946	10.071	11.180	12.330	13.460	14.580	15.700	16.800	17.890	18.970	20.040	21.100	22.150	23.200	24.240	25.280	
38	1.303	1.685	2.845	4.095	5.315	6.536	7.765	8.945	10.070	11.179	12.329	13.459	14.579	15.699	16.799	17.889	18.969	20.039	21.099	22.149	23.199	24.239	25.279	
39	1.303	1.684	2.844	4.094	5.314	6.535	7.764	8.944	10.069	11.178	12.328	13.458	14.578	15.698	16.798	17.888	18.968	20.038	21.098	22.148	23.198	24.238	25.278	
40	1.302	1.683	2.843	4.093	5.313	6.534	7.763	8.943	10.068	11.177	12.327	13.457	14.577	15.697	16.797	17.887	18.967	20.037	21.097	22.147	23.197	24.237	25.277	
41	1.301	1.682	2.842	4.092	5.312	6.533	7.762	8.942	10.067	11.176	12.326	13.456	14.576	15.696	16.796	17.886	18.966	20.036	21.096	22.146	23.196	24.236	25.276	
42	1.300	1.681	2.841	4.091	5.311	6.532	7.761	8.941	10.066	11.175	12.325	13.455	14.575	15.695	16.795	17.885	18.965	20.035	21.095	22.145	23.195	24.235	25.275	
43	1.300	1.680	2.840	4.090	5.310	6.531	7.760	8.940	10.065	11.174	12.324	13.454	14.574	15.694	16.794	17.884	18.964	20.034	21.094	22.144	23.194	24.234	25.274	
44	1.299	1.679	2.839	4.089	5.309	6.530	7.759	8.939	10.064	11.173	12.323	13.453	14.573	15.693	16.793	17.883	18.963	20.033	21.093	22.143	23.193	24.233	25.273	
45	1.298	1.678	2.838	4.088	5.308	6.529	7.758	8.938	10.063	11.172	12.322	13.452	14.572	15.692	16.792	17.882	18.962	20.032	21.092	22.142	23.192	24.232	25.272	
46	1.297	1.677	2.837	4.087	5.307	6.528	7.757	8.937	10.062	11.171	12.321	13.451	14.571	15.691	16.791	17.881	18.961	20.031	21.091	22.141	23.191	24.231	25.271	
47	1.296	1.676	2.836	4.086	5.306	6.527	7.756	8.936	10.061	11.170	12.320	13.450	14.570	15.690	16.790	17.880	18.960	20.030	21.090	22.140	23.190	24.230	25.270	
48	1.295	1.675	2.835	4.085	5.305	6.526	7.755	8.935	10.060	11.169	12.319	13.449	14.569	15.689	16.789	1								

Table A.8 : Curve Test Areas



	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
0.0	500	500	500	500	500	500	500	500	500	500	500	500	500	500	500	500	500	500
0.1	468	465	463	462	462	462	462	461	461	461	461	461	461	461	461	461	461	461
0.2	437	430	427	426	425	424	424	423	423	423	422	422	422	422	422	422	422	422
0.3	406	398	392	390	388	387	386	386	385	385	384	384	384	384	384	384	384	384
0.4	379	364	358	355	353	352	351	350	349	349	348	348	347	347	347	347	347	347
0.5	352	333	326	322	319	317	316	315	314	313	313	313	312	312	312	312	312	312
0.6	328	305	295	290	287	285	284	283	282	281	280	279	279	279	278	278	278	278
0.7	306	278	267	261	258	255	253	252	251	250	249	248	247	247	247	247	247	247
0.8	285	254	241	234	230	227	225	223	221	220	219	218	218	218	218	218	218	218
0.9	265	232	217	210	205	201	199	197	196	195	194	193	192	191	191	191	191	191
1.0	250	211	196	187	182	178	175	172	170	169	168	167	166	165	165	166	166	166
1.1	235	193	176	167	162	157	154	152	150	149	147	146	145	144	144	144	144	145
1.2	221	177	158	148	142	138	135	132	130	129	128	127	126	124	124	124	125	125
1.3	209	162	142	132	125	121	117	115	113	111	110	109	108	107	107	108	108	108
1.4	197	143	122	111	104	99	95	92	89	86	84	82	81	80	79	77	77	77
1.5	186	130	108	97	90	84	80	76	73	70	68	66	65	64	63	62	61	61
1.6	178	125	103	92	85	78	74	70	67	64	62	60	59	57	56	55	54	54
1.7	169	116	94	83	76	69	65	62	59	56	54	53	52	50	49	48	47	47
1.8	161	107	85	74	67	60	56	53	50	47	45	44	43	41	40	39	38	38
1.9	154	99	77	66	59	52	48	45	42	39	37	36	35	33	32	31	30	30
2.0	148	92	70	59	52	45	41	38	35	33	32	31	30	28	27	26	25	25
2.1	141	85	63	52	45	38	34	31	28	26	25	24	23	21	20	19	18	18
2.2	136	79	57	46	39	32	28	25	22	20	19	18	17	15	14	13	12	12
2.3	131	74	52	41	34	27	23	20	17	15	14	13	12	10	9	8	7	7
2.4	126	69	48	37	30	23	19	16	13	11	10	9	8	6	5	4	3	3
2.5	121	65	44	33	26	19	15	12	9	8	7	6	5	3	2	1	0	0
2.6	117	61	40	30	23	16	12	9	7									
2.7	113	57	37	27	20	13	10	7										
2.8	109	54	34	24	17	10	7											
2.9	106	51	31	22	15	8	5											
3.0	102	48	29	20	13	6	4											
3.1	99	45	27	18	11	5	3											
3.2	96	43	25	16	10	4	3											
3.3	94	40	23	15	9	3	2											
3.4	91	38	21	14	8	2	1											
3.5	89	36	20	12	7	1												
3.6	86	33	18	11	6													
3.7	84	31	17	10	5													
3.8	82	30	16	9	4													
3.9	80	28	15	8	3													
4.0	78	27	14	7	2													

Table A.8 † Curve Tail Areas (cont.)

[illegible]

97% Probability and Statistics for Engineers

Table A.9 Critical Values for F Distributions

		α = numerator df												β = denominator df											
		1	2	3	4	5	6	7	8	9	10	12	15	20	25	30	40	50	60	70	80	90	100	120	150
1	.100	39.86	49.80	55.99	57.24	58.20	58.91	59.44	59.86	60.19	60.71	61.22	61.74	62.03	62.26	62.46	62.63	62.79	62.94	63.08	63.21	63.33	63.45	63.57	63.69
	.050	161.45	199.47	215.71	224.58	230.16	233.99	236.77	238.68	240.54	242.35	244.12	245.85	247.54	249.20	250.83	252.44	254.02	255.58	257.12	258.64	260.14	261.62	263.08	264.53
	.010	4021.2	4999.4	5413.4	5624.6	5763.6	5859.0	5928.4	5981.1	6027.5	6068.8	6106.3	6140.9	6172.8	6202.6	6230.6	6256.8	6281.4	6304.6	6326.5	6347.2	6366.8	6385.4	6403.1	6419.9
2	.100	18.51	23.68	26.88	28.24	29.17	29.80	30.28	30.66	31.00	31.31	31.60	31.87	32.12	32.35	32.56	32.75	32.92	33.08	33.23	33.37	33.50	33.63	33.75	33.87
	.050	98.50	124.28	139.49	148.47	154.50	158.99	162.99	166.54	169.68	172.44	174.84	176.91	178.67	180.15	181.47	182.65	183.70	184.72	185.71	186.68	187.62	188.54	189.44	190.32
	.010	999.50	1249.8	1409.9	1509.9	1589.9	1659.9	1719.9	1769.9	1809.9	1849.9	1889.9	1929.9	1969.9	2009.9	2049.9	2089.9	2129.9	2169.9	2209.9	2249.9	2289.9	2329.9	2369.9	2409.9
3	.100	16.69	21.58	24.69	26.46	27.71	28.54	29.14	29.60	30.00	30.37	30.71	31.03	31.33	31.60	31.85	32.09	32.31	32.52	32.72	32.91	33.09	33.26	33.43	33.59
	.050	84.29	106.65	120.90	128.46	134.50	139.49	143.99	147.99	151.44	154.44	157.00	159.24	161.17	162.89	164.41	165.84	167.18	168.53	169.79	171.06	172.33	173.59	174.85	176.11
	.010	989.50	1239.8	1399.9	1499.9	1579.9	1649.9	1709.9	1759.9	1809.9	1849.9	1889.9	1929.9	1969.9	2009.9	2049.9	2089.9	2129.9	2169.9	2209.9	2249.9	2289.9	2329.9	2369.9	2409.9
4	.100	15.99	20.59	23.49	25.09	26.24	27.04	27.64	28.14	28.54	28.94	29.34	29.74	30.14	30.54	30.94	31.34	31.74	32.14	32.54	32.94	33.34	33.74	34.14	34.54
	.050	79.29	100.09	113.09	120.09	125.59	130.09	134.09	137.59	140.59	143.09	145.09	146.99	148.79	150.49	152.09	153.69	155.29	156.89	158.49	159.99	161.49	162.99	164.49	165.99
	.010	979.50	1229.8	1389.9	1489.9	1569.9	1639.9	1699.9	1749.9	1799.9	1839.9	1879.9	1919.9	1959.9	1999.9	2039.9	2079.9	2119.9	2159.9	2199.9	2239.9	2279.9	2319.9	2359.9	2399.9
5	.100	15.59	20.09	22.89	24.39	25.54	26.34	26.94	27.44	27.84	28.24	28.64	29.04	29.44	29.84	30.24	30.64	31.04	31.44	31.84	32.24	32.64	33.04	33.44	33.84
	.050	76.29	96.69	109.29	115.79	120.79	125.29	129.29	132.79	135.79	138.29	140.29	141.99	143.49	144.89	146.19	147.49	148.79	149.99	151.19	152.39	153.59	154.79	155.99	157.19
	.010	969.50	1219.8	1379.9	1479.9	1559.9	1629.9	1689.9	1739.9	1789.9	1829.9	1869.9	1909.9	1949.9	1989.9	2029.9	2069.9	2109.9	2149.9	2189.9	2229.9	2269.9	2309.9	2349.9	2389.9
6	.100	15.29	19.69	22.49	23.99	25.14	25.94	26.54	27.04	27.44	27.84	28.24	28.64	29.04	29.44	29.84	30.24	30.64	31.04	31.44	31.84	32.24	32.64	33.04	33.44
	.050	73.29	93.29	105.49	111.99	116.49	120.99	124.99	128.49	131.49	134.09	136.09	137.79	139.29	140.69	141.99	143.29	144.59	145.89	147.19	148.49	149.79	150.99	152.19	153.39
	.010	959.50	1209.8	1369.9	1469.9	1549.9	1619.9	1679.9	1729.9	1779.9	1819.9	1859.9	1899.9	1939.9	1979.9	2019.9	2059.9	2099.9	2139.9	2179.9	2219.9	2259.9	2299.9	2339.9	2379.9
7	.100	15.09	19.49	22.29	23.79	24.94	25.74	26.34	26.84	27.24	27.64	28.04	28.44	28.84	29.24	29.64	30.04	30.44	30.84	31.24	31.64	32.04	32.44	32.84	33.24
	.050	70.29	90.09	102.09	108.49	112.99	117.49	121.49	124.99	127.99	130.49	132.49	134.09	135.59	136.99	138.29	139.59	140.89	142.19	143.49	144.79	146.09	147.39	148.69	149.99
	.010	949.50	1199.8	1359.9	1459.9	1539.9	1609.9	1669.9	1719.9	1769.9	1809.9	1849.9	1889.9	1929.9	1969.9	2009.9	2049.9	2089.9	2129.9	2169.9	2209.9	2249.9	2289.9	2329.9	2369.9
8	.100	14.89	19.29	22.09	23.59	24.74	25.54	26.14	26.64	27.04	27.44	27.84	28.24	28.64	29.04	29.44	29.84	30.24	30.64	31.04	31.44	31.84	32.24	32.64	33.04
	.050	67.29	86.89	98.69	105.09	109.59	114.09	118.09	121.59	124.59	127.09	129.09	130.69	132.09	133.49	134.79	136.09	137.39	138.69	139.99	141.29	142.59	143.89	145.19	146.49
	.010	939.50	1189.8	1349.9	1449.9	1529.9	1599.9	1659.9	1709.9	1759.9	1799.9	1839.9	1879.9	1919.9	1959.9	1999.9	2039.9	2079.9	2119.9	2159.9	2199.9	2239.9	2279.9	2319.9	2359.9
9	.100	14.69	19.09	21.89	23.39	24.54	25.34	25.94	26.44	26.84	27.24	27.64	28.04	28.44	28.84	29.24	29.64	30.04	30.44	30.84	31.24	31.64	32.04	32.44	32.84
	.050	64.29	83.69	95.29	101.69	106.19	110.69	114.69	118.19	121.19	123.69	125.69	127.29	128.69	129.99	131.29	132.59	133.89	135.19	136.49	137.79	139.09	140.39	141.69	142.99
	.010	929.50	1179.8	1339.9	1439.9	1519.9	1589.9	1649.9	1699.9	1749.9	1789.9	1829.9	1869.9	1909.9	1949.9	1989.9	2029.9	2069.9	2109.9	2149.9	2189.9	2229.9	2269.9	2309.9	2349.9
10	.100	14.49	18.89	21.69	23.19	24.34	25.14	25.74	26.24	26.64	27.04	27.44	27.84	28.24	28.64	29.04	29.44	29.84	30.24	30.64	31.04	31.44	31.84	32.24	32.64
	.050	61.29	80.59	92.09	98.49	102.99	107.49	111.49	114.99	117.99	120.49	122.49	124.09	125.49	126.79	128.09	129.39	130.69	131.99	133.29	134.59	135.89	137.19	138.49	139.79
	.010	919.50	1169.8	1329.9	1429.9	1509.9	1579.9	1639.9	1689.9	1739.9	1779.9	1819.9	1859.9	1899.9	1939.9	1979.9	2019.9	2059.9	2099.9	2139.9	2179.9	2219.9	2259.9	2299.9	2339.9
11	.100	14.29	18.69	21.49	22.99	24.14	24.94	25.54	26.04	26.44	26.84	27.24	27.64	28.04	28.44	28.84	29.24	29.64	30.04	30.44	30.84	31.24	31.64	32.04	32.44
	.050	58.29	77.49	88.89	95.29	99.79	104.29	108.29	111.79	114.79	117.29	119.29	120.89	122.29	123.59	124.89	126.19	127.49	128.79	130.09	131.39	132.69	133.99	135.29	136.59
	.010	909.50	1159.8	1319.9	1419.9	1499.9	1569.9	1629.9	1679.9	1729.9	1769.9	1809.9	1849.9	1889.9	1929.9	1969.9	2009.9	2049.9	2089.9	2129.9	2169.9	2209.9	2249.9	2289.9	2329.9
12	.100	14.09	18.49	21.29	22.79	23.94	24.74	25.34	25.84	26.24	26.64	27.04	27.44	27.84	28.24	28.64	29.04	29.44	29.84	30.24	30.64	31.04	31.44	31.84	32.24
	.050	55.29	74.39	85.69	92.09	96.59	101.09	105.09	108.59	111.59	114.09	116.09	117.69	119.09	120.39	121.69	122.99	124.29	125.59	126.89	128.19	129.49	130.79	132.09	133.39
	.010	899.50	1149.8	1309.9	1409.9	1489.9	1559.9	1619.9	1669.9	1719.9	1759.9	1799.9	1839.9	1879.9	1919.9	1959.9	1999.9	2039.9	2079.9	2119.9	2159.9	2199.9	2239.9	2279.9	2319.9

(continued)

(continued)

Appendix Table 379

Table A.9 Critical Values for F Distributions (cont.)

		α , numerator df										ν , denominator df									
		10	12	15	20	25	30	40	50	60	100	10	12	15	20	25	30	40	50	60	100
13	.005	2.14	2.10	2.05	2.01	1.98	1.95	1.93	1.92	1.90	1.88	1.93	1.90	1.88	1.86	1.84	1.82	1.80	1.78	1.76	1.74
	.010	2.67	2.60	2.53	2.46	2.41	2.38	2.34	2.31	2.28	2.26	2.31	2.28	2.26	2.24	2.22	2.20	2.18	2.16	2.14	2.12
	.050	4.10	3.96	3.82	3.66	3.57	3.51	3.43	3.38	3.34	3.32	3.38	3.34	3.32	3.30	3.28	3.26	3.24	3.22	3.20	3.18
14	.005	6.80	6.52	6.23	5.93	5.75	5.63	5.47	5.37	5.30	5.28	5.33	5.29	5.27	5.25	5.23	5.21	5.19	5.17	5.15	5.13
	.010	2.10	2.05	2.01	1.96	1.93	1.91	1.89	1.87	1.86	1.84	1.89	1.86	1.84	1.82	1.80	1.78	1.76	1.74	1.72	1.70
	.050	2.60	2.53	2.46	2.39	2.34	2.31	2.27	2.24	2.22	2.20	2.27	2.24	2.22	2.20	2.18	2.16	2.14	2.12	2.10	2.08
15	.005	3.94	3.80	3.66	3.51	3.41	3.35	3.27	3.22	3.18	3.16	3.21	3.18	3.16	3.14	3.12	3.10	3.08	3.06	3.04	3.02
	.010	6.40	6.13	5.83	5.53	5.35	5.23	5.07	4.95	4.88	4.86	4.91	4.88	4.86	4.84	4.82	4.80	4.78	4.76	4.74	4.72
	.050	2.08	2.02	1.97	1.92	1.89	1.87	1.85	1.83	1.82	1.80	1.85	1.82	1.80	1.78	1.76	1.74	1.72	1.70	1.68	1.66
16	.005	3.80	3.67	3.52	3.37	3.28	3.23	3.15	3.10	3.06	3.04	3.09	3.06	3.04	3.02	3.00	2.98	2.96	2.94	2.92	2.90
	.010	6.03	5.81	5.54	5.25	5.07	4.95	4.79	4.67	4.60	4.58	4.63	4.60	4.58	4.56	4.54	4.52	4.50	4.48	4.46	4.44
	.050	2.03	1.99	1.94	1.89	1.86	1.84	1.81	1.79	1.78	1.76	1.81	1.78	1.76	1.74	1.72	1.70	1.68	1.66	1.64	1.62
17	.005	2.49	2.42	2.35	2.28	2.23	2.19	2.15	2.12	2.11	2.09	2.14	2.11	2.09	2.07	2.05	2.03	2.01	1.99	1.97	1.95
	.010	3.69	3.53	3.41	3.26	3.16	3.10	3.02	2.97	2.93	2.91	2.96	2.93	2.91	2.89	2.87	2.85	2.83	2.81	2.79	2.77
	.050	5.81	5.55	5.27	4.99	4.82	4.70	4.54	4.43	4.36	4.34	4.39	4.36	4.34	4.32	4.30	4.28	4.26	4.24	4.22	4.20
18	.005	2.00	1.96	1.91	1.86	1.83	1.81	1.78	1.76	1.75	1.73	1.78	1.75	1.73	1.71	1.69	1.67	1.65	1.63	1.61	1.59
	.010	2.45	2.38	2.31	2.25	2.18	2.13	2.08	2.04	2.02	2.00	2.05	2.02	2.00	1.98	1.96	1.94	1.92	1.90	1.88	1.86
	.050	3.39	3.24	3.13	3.03	2.98	2.92	2.84	2.78	2.75	2.73	2.78	2.75	2.73	2.71	2.69	2.67	2.65	2.63	2.61	2.59
19	.005	1.98	1.92	1.89	1.84	1.80	1.78	1.75	1.73	1.72	1.70	1.75	1.72	1.70	1.68	1.66	1.64	1.62	1.60	1.58	1.56
	.010	2.31	2.24	2.17	2.10	2.03	1.97	1.92	1.88	1.86	1.84	1.89	1.86	1.84	1.82	1.80	1.78	1.76	1.74	1.72	1.70
	.050	3.31	3.17	3.05	2.95	2.90	2.84	2.76	2.70	2.67	2.65	2.70	2.67	2.65	2.63	2.61	2.59	2.57	2.55	2.53	2.51
20	.005	1.96	1.91	1.86	1.81	1.78	1.76	1.73	1.71	1.70	1.68	1.73	1.70	1.68	1.66	1.64	1.62	1.60	1.58	1.56	1.54
	.010	2.28	2.21	2.13	2.06	2.01	1.95	1.90	1.86	1.84	1.82	1.87	1.84	1.82	1.80	1.78	1.76	1.74	1.72	1.70	1.68
	.050	3.28	3.15	3.03	2.93	2.88	2.82	2.74	2.68	2.65	2.63	2.68	2.65	2.63	2.61	2.59	2.57	2.55	2.53	2.51	2.49
21	.005	1.94	1.89	1.84	1.79	1.76	1.74	1.71	1.69	1.68	1.66	1.71	1.68	1.66	1.64	1.62	1.60	1.58	1.56	1.54	1.52
	.010	2.24	2.17	2.09	2.02	1.95	1.89	1.84	1.80	1.78	1.76	1.81	1.78	1.76	1.74	1.72	1.70	1.68	1.66	1.64	1.62
	.050	3.24	3.11	2.99	2.89	2.84	2.78	2.70	2.64	2.61	2.59	2.64	2.61	2.59	2.57	2.55	2.53	2.51	2.49	2.47	2.45
22	.005	1.93	1.88	1.83	1.78	1.75	1.73	1.70	1.68	1.67	1.65	1.70	1.67	1.65	1.63	1.61	1.59	1.57	1.55	1.53	1.51
	.010	2.21	2.14	2.06	1.99	1.92	1.86	1.81	1.77	1.75	1.73	1.78	1.75	1.73	1.71	1.69	1.67	1.65	1.63	1.61	1.59
	.050	3.21	3.08	2.96	2.86	2.81	2.75	2.67	2.61	2.58	2.56	2.61	2.58	2.56	2.54	2.52	2.50	2.48	2.46	2.44	2.42
23	.005	1.92	1.87	1.82	1.77	1.74	1.72	1.69	1.67	1.66	1.64	1.69	1.66	1.64	1.62	1.60	1.58	1.56	1.54	1.52	1.50
	.010	2.19	2.12	2.04	1.97	1.90	1.84	1.79	1.75	1.73	1.71	1.76	1.73	1.71	1.69	1.67	1.65	1.63	1.61	1.59	1.57
	.050	3.19	3.06	2.94	2.84	2.79	2.73	2.65	2.59	2.56	2.54	2.59	2.56	2.54	2.52	2.50	2.48	2.46	2.44	2.42	2.40
24	.005	1.91	1.86	1.81	1.76	1.73	1.71	1.68	1.66	1.65	1.63	1.68	1.65	1.63	1.61	1.59	1.57	1.55	1.53	1.51	1.49
	.010	2.17	2.10	2.02	1.95	1.88	1.82	1.77	1.73	1.71	1.69	1.74	1.71	1.69	1.67	1.65	1.63	1.61	1.59	1.57	1.55
	.050	3.17	3.04	2.92	2.82	2.77	2.71	2.63	2.57	2.54	2.52	2.57	2.54	2.52	2.50	2.48	2.46	2.44	2.42	2.40	2.38

Table A.9 Critical Values for F Distributions (cont.)

		α , numerator df										ν , denominator df										
		1	2	3	4	5	6	7	8	9												
13	.005	3.14	2.76	2.56	2.42	2.35	2.28	2.23	2.20	2.16	14	.005	4.07	3.61	3.41	3.27	3.20	3.16	3.12	3.09	3.06	
	.010	4.97	4.50	4.30	4.16	4.09	4.02	3.97	3.94	3.91		.010	5.74	5.27	5.07	4.93	4.86	4.82	4.79	4.76	4.73	
	.050	17.22	12.31	10.21	9.07	8.35	7.86	7.49	7.21	6.98		.050	21.22	15.31	13.21	12.07	11.35	10.86	10.49	10.21	9.98	9.75
14	.005	3.10	2.73	2.52	2.39	2.31	2.24	2.19	2.15	2.12	15	.005	4.60	4.13	3.94	3.79	3.72	3.68	3.64	3.61	3.58	3.55
	.010	5.51	5.04	4.84	4.70	4.63	4.56	4.52	4.49	4.46		.010	6.31	5.84	5.64	5.49	5.42	5.38	5.35	5.32	5.29	
	.050	17.14	11.78	9.73	8.62	7.92	7.44	7.03	6.80	6.58		.050	21.11	15.20	13.10	11.96	11.24	10.75	10.38	10.10	9.87	9.64
15	.005	3.07	2.70	2.49	2.36	2.27	2.21	2.16	2.12	2.09	16	.005	4.54	4.07	3.88	3.73	3.66	3.62	3.58	3.55	3.52	3.49
	.010	5.45	4.98	4.78	4.64	4.57	4.50	4.46	4.43	4.40		.010	6.26	5.79	5.59	5.44	5.37	5.33	5.30	5.27	5.24	
	.050	16.99	11.63	9.58	8.47	7.77	7.29	6.88	6.65	6.42		.050	20.94	15.03	12.93	11.79	11.07	10.58	10.21	9.93	9.70	9.47
16	.005	3.05	2.67	2.46	2.33	2.24	2.18	2.13	2.09	2.06	17	.005	4.49	4.02	3.83	3.68	3.61	3.57	3.53	3.50	3.47	3.44
	.010	5.40	4.93	4.73	4.59	4.52	4.45	4.41	4.38	4.35		.010	6.21	5.74	5.54	5.39	5.32	5.28	5.25	5.22	5.19	
	.050	16.82	10.97	9.01	7.94	7.27	6.80	6.46	6.19	5.98		.050	20.77	14.86	12.76	11.62	10.90	10.41	10.04	9.76	9.53	9.30
17	.005	3.03	2.64	2.44	2.31	2.22	2.15	2.10	2.06	2.03	18	.005	4.45	3.98	3.79	3.64	3.57	3.53	3.49	3.46	3.43	3.40
	.010	5.36	4.89	4.69	4.55	4.48	4.41	4.37	4.34	4.31		.010	6.18	5.71	5.51	5.36	5.29	5.25	5.22	5.19	5.16	
	.050	16.72	10.87	8.91	7.84	7.17	6.70	6.36	6.12	5.96		.050	20.60	14.69	12.59	11.45	10.73	10.24	9.87	9.59	9.36	9.13
18	.005	3.01	2.62	2.42	2.29	2.20	2.13	2.08	2.04	2.00	19	.005	4.41	3.94	3.75	3.60	3.53	3.49	3.45	3.42	3.39	3.36
	.010	5.32	4.85	4.65	4.51	4.44	4.37	4.33	4.30	4.27		.010	6.14	5.67	5.47	5.32	5.25	5.21	5.18	5.15	5.12	
	.050	16.58	10.73	8.77	7.70	7.03	6.56	6.22	5.98	5.75		.050	20.43	14.52	12.42	11.28	10.56	10.07	9.70	9.42	9.19	8.96
19	.005	2.99	2.60	2.40	2.27	2.18	2.11	2.06	2.02	1.98	20	.005	4.37	3.90	3.71	3.56	3.49	3.45	3.41	3.38	3.35	3.32
	.010	5.28	4.81	4.61	4.47	4.40	4.34	4.30	4.27	4.24		.010	6.10	5.63	5.43	5.28	5.21	5.17	5.14	5.11	5.08	
	.050	16.44	10.59	8.63	7.56	6.89	6.42	6.08	5.84	5.61		.050	20.21	14.30	12.20	11.06	10.34	9.85	9.48	9.20	8.97	8.74
20	.005	2.97	2.57	2.36	2.23	2.14	2.07	2.02	1.98	1.94	21	.005	4.33	3.86	3.67	3.52	3.45	3.41	3.37	3.34	3.31	3.28
	.010	5.24	4.77	4.57	4.43	4.36	4.30	4.26	4.23	4.20		.010	6.07	5.60	5.40	5.25	5.18	5.14	5.11	5.08	5.05	
	.050	16.30	10.45	8.49	7.42	6.75	6.28	5.94	5.70	5.47		.050	20.02	14.11	12.01	10.87	10.15	9.66	9.29	9.01	8.78	8.55
21	.005	2.96	2.55	2.34	2.21	2.11	2.04	2.00	1.96	1.92	22	.005	4.30	3.83	3.64	3.49	3.42	3.38	3.34	3.31	3.28	3.25
	.010	5.21	4.74	4.54	4.40	4.33	4.27	4.23	4.20	4.17		.010	6.04	5.57	5.37	5.22	5.15	5.11	5.08	5.05	5.02	
	.050	16.16	10.31	8.35	7.28	6.61	6.14	5.80	5.56	5.33		.050	19.83	13.92	11.82	10.68	9.96	9.47	9.10	8.82	8.59	8.36
22	.005	2.95	2.54	2.33	2.20	2.10	2.03	1.99	1.95	1.92	23	.005	4.28	3.81	3.62	3.47	3.40	3.36	3.32	3.29	3.26	3.23
	.010	5.18	4.71	4.51	4.37	4.30	4.24	4.20	4.17	4.14		.010	6.01	5.54	5.34	5.19	5.12	5.08	5.05	5.02	4.99	
	.050	16.02	10.17	8.21	7.14	6.47	6.00	5.66	5.42	5.19		.050	19.64	13.73	11.63	10.49	9.77	9.28	8.91	8.63	8.40	8.17
23	.005	2.94	2.53	2.32	2.19	2.09	2.02	1.98	1.94	1.91	24	.005	4.26	3.79	3.60	3.45	3.38	3.34	3.30	3.27	3.24	3.21
	.010	5.15	4.68	4.48	4.34	4.27	4.21	4.17	4.14	4.11		.010	5.99	5.52	5.32	5.17	5.10	5.06	5.03	5.00	4.97	
	.050	15.88	10.03	8.07	7.00	6.33	5.86	5.52	5.28	5.05		.050	19.45	13.54	11.44	10.30	9.58	9.09	8.72	8.44	8.21	7.98
24	.005	2.93	2.52	2.31	2.18	2.08	2.01	1.97	1.93	1.90	25	.005	4.23	3.76	3.57	3.42	3.35	3.31	3.27	3.24	3.21	3.18
	.010	5.12	4.65	4.45	4.31	4.24	4.18	4.14	4.11	4.08		.010	5.96	5.49	5.29	5.14	5.07	5.03	5.00	4.97	4.94	
	.050	15.73	9.88	7.92	6.85	6.18	5.71	5.37	5.13	4.90		.050	19.26	13.35	11.25	10.11	9.39	8.90	8.53	8.25	8.02	7.79

Table A.9 Critical Values for P Distributions (cont.)

		$P_1 = \text{area under } P_1$									
		1	2	3	4	5	6	7	8	9	
25	.100	2.92	2.53	2.32	2.18	2.09	2.03	1.97	1.93	1.89	
	.050	4.34	3.59	3.22	2.76	2.60	2.49	2.40	2.34	2.28	
	.010	13.77	9.37	7.45	5.65	5.09	4.63	4.30	4.05	3.85	
	.001	31.83	19.37	14.66	10.98	9.59	8.44	7.63	7.00	6.50	
	.000	43.33	25.81	19.50	14.00	12.15	10.54	9.39	8.55	7.88	
30	.100	2.58	2.22	2.03	1.88	1.80	1.74	1.68	1.64	1.60	
	.050	3.77	3.09	2.74	2.31	2.16	2.05	1.96	1.90	1.84	
	.010	11.99	7.88	6.00	4.41	3.95	3.58	3.26	3.01	2.78	
	.001	28.43	16.27	12.15	8.56	7.33	6.39	5.69	5.14	4.70	
	.000	37.45	21.01	15.58	11.15	9.69	8.44	7.44	6.66	6.00	
35	.100	2.35	2.02	1.84	1.69	1.61	1.55	1.50	1.46	1.42	
	.050	3.49	2.85	2.51	2.09	1.94	1.83	1.74	1.68	1.62	
	.010	11.15	7.23	5.40	3.92	3.46	3.10	2.78	2.53	2.30	
	.001	26.84	15.09	11.00	7.70	6.56	5.62	4.92	4.37	3.93	
	.000	35.81	19.59	14.26	9.84	8.38	7.13	6.13	5.35	4.69	
40	.100	2.15	1.84	1.67	1.52	1.44	1.38	1.33	1.29	1.25	
	.050	3.28	2.67	2.34	1.93	1.78	1.67	1.58	1.52	1.46	
	.010	10.55	6.75	5.03	3.64	3.18	2.82	2.50	2.25	2.02	
	.001	25.01	14.00	10.00	6.90	5.76	4.82	4.12	3.57	3.13	
	.000	33.99	17.97	12.64	8.22	6.76	5.51	4.51	3.73	3.07	
45	.100	1.98	1.68	1.51	1.36	1.28	1.22	1.17	1.13	1.09	
	.050	3.12	2.52	2.20	1.80	1.65	1.54	1.45	1.39	1.33	
	.010	10.00	6.35	4.73	3.35	2.89	2.53	2.21	1.96	1.72	
	.001	23.68	13.15	9.33	6.25	5.11	4.17	3.47	2.92	2.48	
	.000	32.65	17.12	11.79	7.37	5.91	4.66	3.66	2.88	2.22	
50	.100	1.83	1.54	1.37	1.22	1.14	1.08	1.03	0.99	0.95	
	.050	2.97	2.38	2.06	1.67	1.52	1.41	1.32	1.26	1.20	
	.010	9.59	6.04	4.42	3.05	2.59	2.23	1.91	1.66	1.42	
	.001	22.28	11.75	8.03	5.05	3.91	3.07	2.37	1.82	1.38	
	.000	31.23	16.10	10.77	6.35	4.89	3.64	2.64	1.86	1.20	
60	.100	1.68	1.39	1.22	1.07	0.99	0.93	0.88	0.84	0.80	
	.050	2.81	2.23	1.91	1.52	1.37	1.26	1.17	1.11	1.05	
	.010	9.15	5.60	4.00	2.63	2.17	1.81	1.49	1.24	0.99	
	.001	21.00	10.47	6.75	3.77	2.63	1.79	1.09	0.74	0.30	
	.000	30.00	15.34	10.01	5.59	4.13	2.88	1.88	1.10	0.44	
70	.100	1.54	1.25	1.08	0.93	0.85	0.79	0.74	0.70	0.66	
	.050	2.65	2.07	1.75	1.36	1.21	1.10	1.01	0.95	0.89	
	.010	8.79	5.24	3.64	2.27	1.81	1.45	1.13	0.88	0.63	
	.001	20.00	9.47	5.75	2.77	1.63	0.93	0.68	0.43	0.18	
	.000	29.00	14.21	8.88	4.41	2.95	1.70	0.92	0.37	0.01	
80	.100	1.41	1.12	0.95	0.80	0.72	0.66	0.61	0.57	0.53	
	.050	2.50	1.92	1.60	1.21	1.06	0.95	0.86	0.80	0.74	
	.010	8.44	4.89	3.30	1.93	1.47	1.11	0.79	0.54	0.29	
	.001	19.00	8.47	4.75	1.77	0.97	0.62	0.37	0.12	0.00	
	.000	28.00	13.00	7.67	3.20	1.74	0.87	0.22	0.00	0.00	
90	.100	1.28	1.00	0.83	0.68	0.60	0.54	0.49	0.45	0.41	
	.050	2.35	1.77	1.45	1.06	0.91	0.80	0.71	0.65	0.59	
	.010	8.10	4.55	2.96	1.59	1.13	0.77	0.45	0.20	0.00	
	.001	18.00	7.44	3.72	1.40	0.74	0.39	0.17	0.00	0.00	
	.000	27.00	11.79	6.46	2.40	0.95	0.30	0.00	0.00	0.00	
100	.100	1.15	0.87	0.70	0.55	0.47	0.41	0.36	0.32	0.28	
	.050	2.20	1.62	1.30	0.91	0.76	0.65	0.56	0.50	0.44	
	.010	7.71	4.16	2.57	1.20	0.74	0.38	0.16	0.00	0.00	
	.001	17.00	6.35	2.80	0.90	0.35	0.00	0.00	0.00	0.00	
	.000	26.00	10.47	4.90	1.30	0.20	0.00	0.00	0.00	0.00	

(continued)

Table A.10 Critical Values for P Distributions (cont.)

		$P_1 = \text{area under } P_1$									
		10	12	15	20	25	30	40	50	60	100
25	.100	1.87	1.83	1.77	1.72	1.68	1.65	1.63	1.61	1.59	1.52
	.050	2.24	2.16	2.09	2.01	1.96	1.92	1.87	1.84	1.82	1.72
	.010	3.13	2.99	2.85	2.70	2.60	2.54	2.45	2.40	2.36	2.18
	.001	4.56	4.31	4.06	3.79	3.63	3.52	3.37	3.28	3.22	2.91
	.000	5.88	5.53	5.18	4.79	4.57	4.41	4.21	4.08	3.98	3.64
30	.100	1.86	1.81	1.76	1.71	1.67	1.65	1.63	1.61	1.59	1.51
	.050	2.22	2.15	2.07	1.99	1.94	1.90	1.85	1.82	1.80	1.70
	.010	3.11	2.96	2.82	2.66	2.57	2.50	2.40	2.35	2.31	2.12
	.001	4.48	4.24	3.99	3.72	3.56	3.44	3.30	3.21	3.15	2.84
	.000	5.80	5.45	5.10	4.71	4.49	4.33	4.13	3.99	3.89	3.54
35	.100	1.85	1.80	1.75	1.70	1.66	1.64	1.62	1.60	1.58	1.50
	.050	2.20	2.13	2.05	1.97	1.92	1.88	1.84	1.81	1.79	1.68
	.010	3.09	2.93	2.78	2.63	2.54	2.47	2.35	2.31	2.28	2.08
	.001	4.41	4.17	3.92	3.65	3.49	3.38	3.23	3.14	3.08	2.76
	.000	5.73	5.38	5.03	4.64	4.42	4.26	4.06	3.92	3.82	3.47
40	.100	1.84	1.79	1.74	1.69	1.65	1.63	1.61	1.59	1.57	1.48
	.050	2.19	2.12	2.04	1.96	1.91	1.87	1.83	1.80	1.78	1.66
	.010	3.07	2.90	2.75	2.60	2.51	2.44	2.32	2.28	2.25	2.03
	.001	4.39	4.15	3.90	3.63	3.47	3.36	3.21	3.12	3.06	2.72
	.000	5.70	5.35	5.00	4.61	4.39	4.23	4.03	3.89	3.79	3.44
45	.100	1.83	1.78	1.73	1.68	1.64	1.62	1.60	1.58	1.55	1.47
	.050	2.18	2.10	2.03	1.94	1.89	1.85	1.81	1.78	1.75	1.63
	.010	3.05	2.88	2.73	2.57	2.48	2.41	2.29	2.25	2.22	2.00
	.001	4.36	4.12	3.87	3.60	3.44	3.33	3.18	3.09	3.03	2.68
	.000	5.68	5.33	4.98	4.59	4.37	4.21	4.01	3.87	3.77	3.42
50	.100	1.82	1.77	1.72	1.67	1.63	1.61	1.59	1.57	1.55	1.46
	.050	2.16	2.09	2.01	1.93	1.88	1.84	1.80	1.77	1.74	1.62
	.010	3.03	2.86	2.71	2.55	2.46	2.39	2.27	2.23	2.20	1.97
	.001	4.34	4.10	3.85	3.58	3.42	3.31	3.16	3.07	3.01	2.66
	.000	5.66	5.31	4.96	4.57	4.35	4.19	3.99	3.85	3.75	3.40
60	.100	1.81	1.76	1.71	1.66	1.62	1.60	1.58	1.56	1.54	1.45
	.050	2.15	2.08	2.00	1.92	1.87	1.83	1.79	1.76	1.73	1.61
	.010	2.99	2.82	2.67	2.51	2.42	2.35	2.23	2.19	2.16	1.93
	.001	4.32	4.08	3.83	3.56	3.40	3.29	3.14	3.05	2.99	2.64
	.000	5.64	5.29	4.94	4.55	4.33	4.17	3.97	3.83	3.73	3.38
70	.100	1.80	1.75	1.70	1.65	1.61	1.59	1.57	1.55	1.53	1.44
	.050	2.14	2.07	1.99	1.91	1.86	1.82	1.78	1.75	1.72	1.60
	.010	2.97	2.80	2.65	2.49	2.40	2.33	2.21	2.17	2.14	1.91
	.001	4.30	4.06	3.81	3.54	3.38	3.27	3.12	3.03	2.97	2.62
	.000	5.62	5.27	4.92	4.53	4.31	4.15	3.95	3.81	3.71	3.36
80	.100	1.79	1.74	1.69	1.64	1.60	1.58	1.56	1.54	1.52	1.43
	.050	2.13	2.06	1.98	1.90	1.85	1.81	1.77	1.74	1.71	1.59
	.010	2.95	2.78	2.63	2.47	2.38	2.31	2.19	2.15	2.12	1.89
	.001	4.28	4.04	3.79	3.52	3.36	3.25	3.10	3.01	2.95	2.60
	.000	5.60	5.25	4.90	4.51	4.29	4.13	3.93	3.79	3.69	3.34
90	.100	1.78	1.73	1.68	1.63	1.59	1.57	1.55	1.53	1.51	1.42
	.050	2.12	2.05	1.97	1.89	1.84	1.80	1.76	1.73	1.70	1.58
	.010	2.93	2.76	2.61	2.45	2.36	2.29	2.17	2.13	2.10	1.87
	.001	4.26	4.02	3.77	3.50	3.34	3.23	3.08	2.99	2.93	2.58
	.000	5.58	5.23	4.88	4.49	4.27	4.11	3.91	3.77	3.67	3.32

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